SUBRACTION

Reception:

EHLT are implementing Mastering Number at Reception in September 2024.



The programme aims to secure firm foundations in the development of good number sense for all children from Reception through to Year 1 and Year 2. The aim over time is that children will leave KS1 with fluency in calculation and a confidence and flexibility with number. Attention will be given to key knowledge and understanding needed in Reception classes, and progression through KS1 to support success in the future. Over the year, the children will experience using a range of resources and representations.

Research shows that children with secure 'number sense' early on will make more progress later on in maths and across the curriculum.

	SUBTRACTION KEY VOCABULARY						
Year 1	Year 2	Year 3	Year 4	Year 5	Year 6		
Equal to; take; take away; take from; less; minus; subtract; leaves; how many more; how many fewer; less than; most; least; count back; how many left; how much less is	Equal to; take; take away; take from; less; minus; subtract; leaves; distance between; difference between; how many more; how many fewer; less than; most; least; count back; how many left; how much less is; difference; count on; strategy; partition; tens; ones	Equal to; take; take away; take from; less; minus; subtract; leaves; distance between; difference between; how many more; how many fewer; less than; most; least; count back; how many left; how much less is; difference; count on; strategy; partition; tens; ones; taking; decrease; hundreds; value; digit	Equal to; take; take away; take from; less; minus; subtract; leaves; distance between; difference between; how many more; how many fewer; less than; most; least; count back; how many left; how much less is; difference; count on; strategy; partition; tens; ones; taking; decrease; hundreds; value; digit; inverse; thousand; exchanges; regroup	Equal to; take; take away; take from; less; minus; subtract; leaves; distance between; difference between; how many more; how many fewer; less than; most; least; count back; how many left; how much less is; difference; count on; strategy; partition; tens; ones; taking; decrease; hundreds; value; digit; inverse; thousand; exchanges; regroup; tenths; hundredths; decimal point; decimal	Equal to; take; take away; take from; less; minus; subtract; leaves; distance between; difference between; how many more; how many fewer; less than; most; least; count back; how many left; how much less is; difference; count on; strategy; partition; tens; ones; taking; decrease; hundreds; value; digit; inverse; thousand; exchanges; regroup; tenths; hundredths; decimal		

^{*}This vocabulary is not an exhaustive list. Teachers will use recommended NCETM vocabulary in lessons.



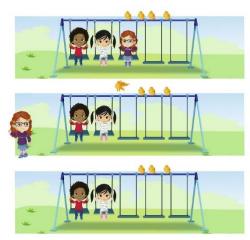


REAL-LIFE REPRESENTATION OTHER REPRESENTATION Comparing Children line up objects to compare the amount. They line the objects up Children line up cubes or counters to compare the amount in either horizontally or vertically. each group. Lines can either be horizontal or vertical. A groups starting line helps to line the objects accurately. There are more yellow cubes. There are fewer red cubes. Ella has more conkers. Tom has fewer conkers.



Counting back and taking away (within 5)

Children remove one more person or object from a group to find one less.

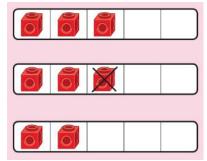


First, there were 3 children.

Then, 1 child left.

Now, there are 2 children.

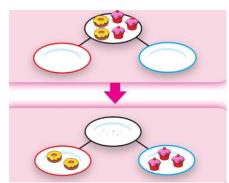
Children use five frames and objects to make a number. They then remove or cross out one object to find one less.



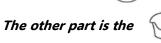
One less than 3 is 2.

Introducing the part-whole model

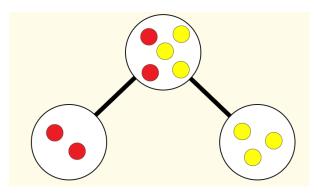
Children sort everyday objects into parts.



One part is the



Children use counters or cubes to represent objects in a partwhole model.

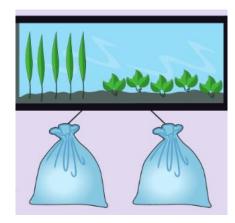


The whole is 5. 2 is a part. 3 is a part.



Finding number bonds to 10

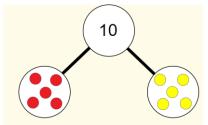
Children partition 10 into different groups to find the number bonds to 10.



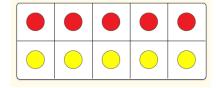
Children begin to work with subtraction number bonds. They break apart 10 to identify different number bonds to 10.



10 are bouncing. 2 get off. 8 are left. 10 - 2 = 8 Children use part-whole models, ten frames and counters to find the number bonds to 10.

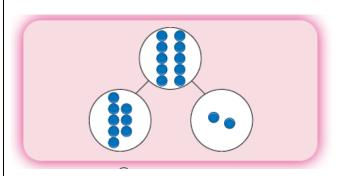


10 is the whole.
5 is a part and 5 is a part.



10 is the whole.
5 is a part and 5 is a part.

Children use part-whole models, and counters to find missing parts and the subtraction number bonds to 10.

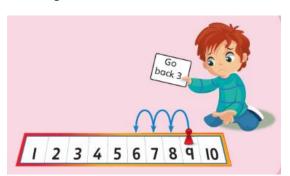


The parts are 8 and 2. 10 is the whole.



Counting back and taking away (number track)

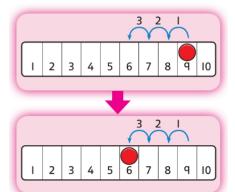
Children use game boards and human number tracks to subtract by counting back.



9 take away 3 equals 6

9...8...7...6

Children use a number track and a counter. They start at the larger number and count back the smaller number to find the answer.

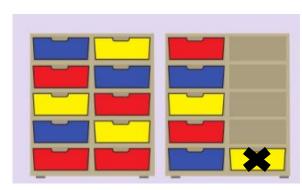


9 take away 3 equals 6

9...8...7...6

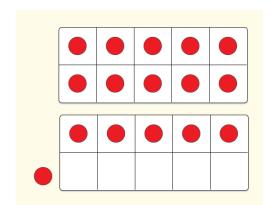
Counting back and taking away (ten frames)

Children count backwards to find one less with numbers up to 20.



One less than 16 is 15.

Children remove counters from ten frames to support in counting back with numbers up to 20.



One less than 16 is 15.

YEAR 1 SUBRACTION



	CONCRETE	PICTORIAL	ABSTRACT
Counting back and taking away	Children arrange objects and remove to find how many are left.	Children draw and cross out or use counters to represent objects from a problem.	Children count back to take away and use a number line or number track to support the method.
			876
	1 less than 6 is 5. 6 subtract 1 is 5.	q – = = There are children left.	0 1 2 3 4 5 6 7 8 9 10
Finding a	Children separate a whole into parts and	Children represent a whole and a part and	9 - 3 = 6 Children use a part-whole model to support
missing part,	understand how one part can be found by	understand how to find the missing part by	the subtraction to find a missing part.
given a whole	subtraction.	subtraction.	
and a part			7
			7 – 3 = ? Children develop an understanding of the relationship between addition and
		5 - 4 =	subtraction facts in a part-whole model.
	8 - 5 = ?		- = - + = - + = - + = - + = - + = - + = - + = - + + = - + + = - + + + = - + + + +



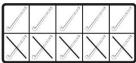
So, 19 - 14 = 5

			Learning Trust
Finding the difference	Arrange two groups so that the difference between the groups can be worked out.	Represent objects using sketches or counters to support finding the difference.	Children understand 'find the difference' as subtraction.
			0 1 2 3 4 5 6 7 8 9 10 10 - 4 = 6
I	8 is 2 more than 6.	5 - 4 = 1	The difference between 10 and 6 is 4.
	6 is 2 less than 8.	The difference between 5 and 4 is 1.	
	The difference between 8 and 6 is 2.		
Subtraction	Understand when and how to subtract 1s	Understand when and how to subtract 1s	Understand how to use knowledge of bonds
within 20	efficiently.	efficiently.	within 10 to subtract efficiently.
	Use a bead string to subtract 1s efficiently.		5 - 3 = 2 15 - 3 = 12
		5 - 3 = 2	
	5 - 3 = 2	15 - 3 = 12	
	15 - 3 = 12	13 - 3 - 12	
Subtracting 10s and 1s	For example: 18 – 12	For example: 18 – 12	Use a part-whole model to support the calculation.
	Subtract 12 by first subtracting the 10, then the remaining 2.	Use ten frames to represent the efficient method of subtracting 12.	14
			10 4 19 - 14 19 - 10 = 9
	First subtract the 10, then take away 2.	First subtract the 10, then subtract 2.	19 - 10 = 9 9 - 4 = 5 So. 19 - 14 = 5



Subtraction bridging 10 using number bonds For example: 12 - 7

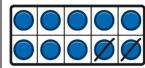
Arrange objects into a 10 and some 1s, then decide on how to split the 7 into parts.

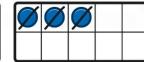




7 is 2 and 5, so I take away the 2 and then the 5.

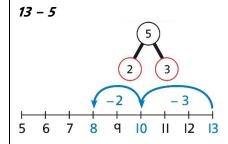
Represent the use of bonds using ten frames.





For 13 – 5, I take away 3 to make 10, then take away 2 to make 8.

Use a number line and a part-whole model to support the method.





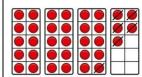


	CONCRETE	PICTORIAL	ABSTRACT
Subtracting multiples of 10	Use known number bonds and unitising to subtract multiples of 10.	Use known number bonds and unitising to subtract multiples of 10.	Use known number bonds and unitising to subtract multiples of 10.
		100	7 70 70 2 5 20 50
	8 subtract 6 is 2. So, 8 tens subtract 6 tens is 2 tens.	10 - 3 = 7 So, 10 tens subtract 3 tens is 7 tens.	7 tens subtract 5 tens is 2 tens. 70 - 50 = 20
Subtracting a single-digit number	Subtract the 1s. This may be done in or out of a place value grid.	Subtract the 1s. This may be done in or out of a place value grid.	Subtract the 1s. Understand the link between counting back and subtracting the 1s using known bonds. 30 31 32 33 34 35 36 37 38 39 40
	T O	T O	$ \begin{array}{c c} \hline & T & O \\ \hline & 3 & q \\ \hline & - & 3 \\ \hline & 3 & 6 \\ \hline & 9 - 3 = 6 \\ & 39 - 3 = 36 \end{array} $

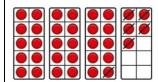


Subtracting	į
single-digit	
number	
bridging 10	

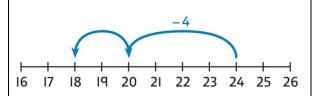
Bridge 10 by using known bonds.



35 – 6 I took away 5 counters, then 1 more. Bridge 10 by using known bonds.

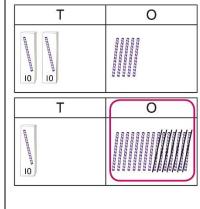


35 - 6 First, I will subtract 5, then 1. Bridge 10 by using known bonds.

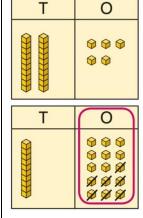


Subtracting a single-digit number using exchange

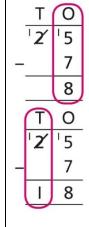
Exchange 1 ten for 10 ones. This may be done in or out of a place value grid.



Exchange 1 ten for 10 ones.



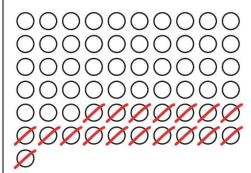
Exchange 1 ten for 10 ones.





Subtracting a 2-digit number

Subtract by taking away.



61 – 18 I took away 1 ten and 8 ones.

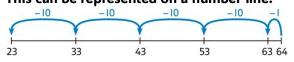
Subtract the 10s and the 1s.

This can be represented on a 100 square.

1	2	3	4	5	6	7	8	9	10
П	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	148	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
٩I	92	93	94	95	96	97	98	99	100

Subtract the 10s and the 1s.

This can be represented on a number line.



$$64 - 1 = 63$$

$$63 - 40 = 23$$

Subtracting a 2-digit number using place value and columns

Subtract the 1s. Then subtract the 10s. This may be done in or out of a place value grid.

Т	0
955550 955550	

38 - 16 = 22

Subtract the 1s. Then subtract the 10s.

Tens	Ones

Using column subtraction, subtract the 1s. Then subtract the 10s.





Subtracting a 2-digit number with exchange	Exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s.	Tens Ones	Using column subtraction, exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s.	T O 4 5 - 2 7
		Tens Ones		T O 3/4 15 - 2 7 T O
		Tens Ones		$ \begin{array}{c c} T & O \\ \hline ^{3}\cancel{4} & ^{1}5 \\ -2 & 7 \\ \hline & 8 \end{array} $
		Tens Ones		$ \begin{array}{c cccc} & T & O \\ \hline & 3 \cancel{4} & 15 \\ & -2 & 7 \\ \hline & 1 & 8 \end{array} $





	CONCRETE	PICTORIAL	ABSTRACT
Subtracting 100s	Use known facts and unitising to subtract multiples of 100.	Use known facts and unitising to subtract multiples of 100.	Understand the link with counting back in 100s.
	100 bricks bricks 100 bricks bricks 5 - 2 = 3 500 - 200 = 300	4 - 2 = 2 400 - 200 = 200	Use known facts and unitising as efficient and accurate methods. I know that 7 - 4 = 3. Therefore, I know that 700 - 400 = 300.
3-digit number – 1s, no exchange	Use number bonds to subtract the 1s.	Use number bonds to subtract the 1s.	Understand the link with counting back using a number line. Use known number bonds to calculate mentally. 476 - 4 = ?
	214 - 3 = ? 10 LOLLIES 10 LOLLIES	319 - 4 = ? H T O O O N O N O O N O O N O O N O O N O O N O O N O O N O O N O O N O O O N O O O N O	476 400 70 6 6 - 4 = 2 476 - 4 = 472
	4 - 3 = 1 214 - 3 = 211	9 - 4 = 5 319 - 4 = 315	



3-digit
number – 1s,
exchange or
bridging
required

Understand why an exchange is necessary by exploring why 1 ten must be exchanged.

Use place value equipment.

Represent the required exchange on a place value grid.

_		
Н	Т	0
Н	Т	0
		ZZZZZ

Calculate mentally by using known bonds.

$$151 - 1 - 5 = 145$$

3-digit number – 10s, no exchange

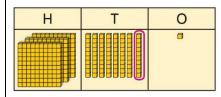
Subtract the 10s using known bonds.



381 - 10 = ?

8 tens with 1 removed is 7 tens.

Subtract the 10s using known bonds.

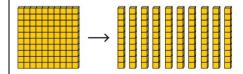


8 tens - 1 ten = 7 tens 381 - 10 = 371 Use known bonds to subtract the 10s mentally.

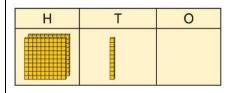


3-digit number - 10s. exchange or bridging required

Use equipment to understand the exchange of 1 hundred for 10 tens.



Represent the exchange on a place value grid using equipment.

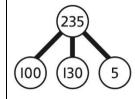


I need to exchange 1 hundred for 10 tens, to help subtract 2 tens.

Н	Т	0

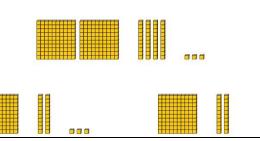
Understand the link with counting back on a number line.

Use flexible partitioning to support the calculation.

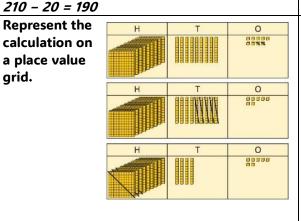


3-digit number - up to 3-digit number

Use place value equipment to explore the effect of splitting a whole into two parts, and understand the link with taking away.



Represent the calculation on a place value grid.



Use column subtraction to calculate accurately and efficiently.

	q	q	q
_	3	5	2
			7
	Н	Т	0
	q	q	9
_	3	5	2
		4	7
	Н	Т	0
	q	q	9
-	3	5	2
	6	4	7

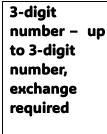
H T O

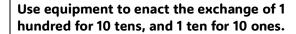


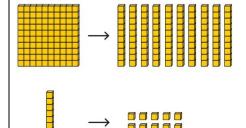
HTO

5 0 6

3 2 8

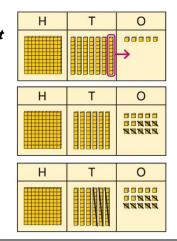






Model the required exchange on a place value grid.

175 - 38 = ?
I need to subtract
8 ones, so I will
exchange a ten
for 10 ones.



Use column subtraction to work accurately and efficiently.

If the subtraction is a 3-digit number subtract a 2-digit number, children should understand how the recording relates to the place value, and so how to line up the digits correctly. $\frac{H \quad T \quad O}{I \quad ^6 \lambda \quad ^{15}}$

Children should also understand how to exchange in calculations where there is a zero in the 10s column.

Representing subtraction problems

Use bar models to represent subtractions.

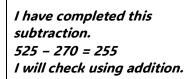
'Find the difference' is represented as two bars for comparison.

Bar models can also be used to show that a part must be taken away from the whole.

Children use alternative representations to check calculations and choose efficient methods.

Children use inverse operations to check additions and subtractions.

The part-whole model supports understanding.











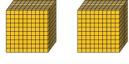
	CONCRETE	PICTORIAL	ABSTRACT
Choosing mental methods where appropriate	Use place value equipment to justify mental methods. What number will be left if we take away 300?	Use place value grids to support mental methods where appropriate. Th H T O O O O O O O O O O O O O O O O O O	Use knowledge of place value and unitising to subtract mentally where appropriate. 3,501 - 2,000 3 thousands - 2 thousands = 1 thousand 3,501 - 2,000 = 1,501
Column subtraction with exchange	Understand why exchange of a 1,000 for 100s, a 100 for 10s, or a 10 for 1s may be necessary.	Represent place value equipment on a place value grid to subtract, including exchanges where needed. The Horizontal The Horiz	Use column subtraction, with understanding of the place value of any exchange required. The Heat To O I 2 5 0 O O O O O O O O O O O O O O O O O O



Column
subtraction
with exchange
across more
than one
column

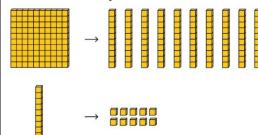
Understand why two exchanges may be necessary.

2,502 - 243 = ?



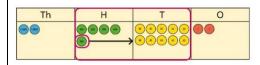


I need to exchange a 10 for some 1s, but there are not any 10s here.



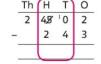
Make exchanges across more than one column where there is a zero as a place holder.

2,502 - 243 = ?



Th	Н	Т	0
			

Make exchanges across more than one column where there is a zero as a place holder.



	Th	Н	T	0
	2	48	٩'ø	12
-		2	4	3
		- Q		

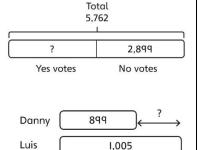
Th	Н	Т	0
2	48	٩¹ø	12
	2	4	3
2	2	5	q

Representing subtractions and checking strategies

Use bar models to represent subtractions where a part needs to be calculated.

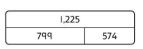
I can work out the total number of Yes votes using 5,762 – 2,899.

Bar models can
also represent
'find the Luis
difference' as a
subtraction problem.



Use inverse operations to check subtractions.

I calculated 1,225 - 799 = 574. I will check by adding the parts.



The parts do not add to make 1,225.

I must have made a mistake.





	CONCRETE	PICTORIAL	ABSTRACT
Column subtraction with whole numbers	Use place value equipment to understand where exchanges are required. 2,250 – 1,070	Represent the stages of the calculation using place value equipment on a grid alongside the calculation, including exchanges where required.	Use column subtraction methods with exchange where required. TTh Th H T O S
		15,735 - 2,582 = 13,153 TTh Th H T O TTh Th H T O 1 5 7 3 5 - 2 5 8 2	
		Now subtract the I0s. Exchange I hundred for I0 tens.	
Checking strategies and representing subtractions		Bar models represent subtractions in problem contexts, including 'find the difference'. Athletics Stadium 75,450 Hockey Centre 42,300 Velodrome 15,735	Children can explain the mistake made when the columns have not been ordered correctly. Bella's working Th Th H T O
			I calculated 18,000 + 4,000 mentally to check my subtraction.



Choosing efficient methods			To subtract two large numbers that are close, children find the difference by counting on. 2,002 - 1,995 = ? Use addition to check subtractions. I calculated 7,546 - 2,355 = 5,191. I will check using the inverse.
Subtracting decimals	Explore complements to a whole number by working in the context of length. O:49 m I m -	Use a place value grid to represent the stages of column subtraction, including exchanges where required. 5.74 - 2.25 = ? O Tth Hth 5 7 4 -2 2 2 5 . Exchange I tenth for I0 hundredths. O Tth Hth 5 67 14 -2 2 2 5 . Now subtract the 5 hundredths. O Tth Hth 5 67 14 -2 2 2 5 . Now subtract the 2 tenths, then the 2 ones. O Tth Hth 5 67 14 -2 2 2 5 . Now subtract the 2 tenths, then the 2 ones.	Use column subtraction, with an understanding of place value, including subtracting numbers with different numbers of decimal places. 3.921 - 3.75 = ? O Tth Hth Thth 3 Q Q I - 3 7 5 0





	CONCRETE	PICTORIAL	ABSTRACT
Comparing and selecting efficient methods	Use counters on a place value grid to represent subtractions of larger numbers. The Harmonian To O O O O O O O O O O O O O O O O O O	Compare subtraction methods alongside place value representations. The Heat Tolday 1 and Tolday	Compare and select methods. Use column subtraction when mental methods are not efficient. Use two different methods for one calculation as a checking strategy. The Heat Toldon Strategy Strategy. Use column subtraction for decimal problems, including in the context of measure. Heat Toldon Strategy
Subtracting mentally with larger numbers		Use a bar model to show how unitising can support mental calculations. 950,000 - 150,000 That is 950 thousands - 150 thousands 950 950 So, the difference is 800 thousands. 950,000 - 150,000 = 800,000	Subtract efficiently from powers of 10. 10,000 - 500 = ?